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# Evaluation of MU-MIMO Digital Beamforming Algorithms in B5G/6G LEO Satellite Systems

**M.R. Dakkak, D.G. Riviello , A. Guidotti , A. Vanelli-Coralli**

Department of Electrical, Electronic and Information Engineering «Guglielmo Marconi»

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The integration of the (**NTNs**) component within the 5G (**NR**) terrestrial ecosystem is to

- improve the system flexibility, adaptability, and resilience
- extend the 5G coverage
- satisfy the high user demand

To this aim ➡ efficient exploitation of the spectrum:

1. By adding unused or underused spectrum chunks by means of flexible spectrum usage paradigms (Cognitive Radio solutions)
  2. Or by decreasing the frequency reuse factor down to full frequency reuse (**FFR**) in **multi-beam systems**.
- The more aggressive frequency reuse (FFR) ➡ the more improvement of the system spectral efficiency
  - The main transmission techniques that allow to use FFR are the advanced precoding/**beamforming techniques** for MU-MIMO schemes.



- The latency between the channel/location estimation phase and the transmission phase:

$$\Delta t = t_1 - t_0$$

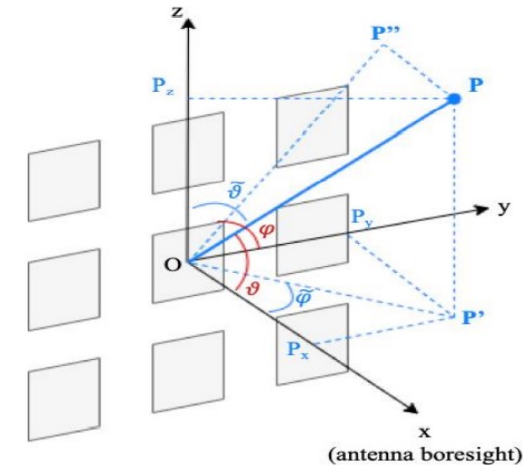
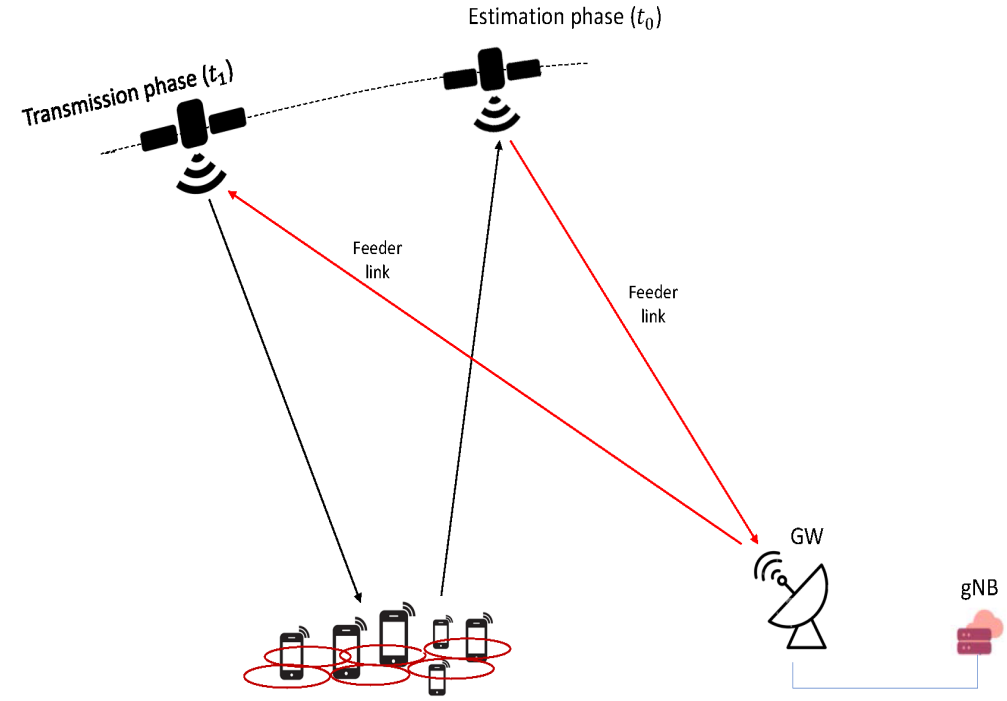
$$= t_{ut,max} + 2t_{feeder} + t_p + t_{ad}$$

- The Channel coefficients:

$$h_{i,n} = g_{i,n}^{(tx)} g_{i,n}^{(rx)} \frac{\lambda}{4\pi d_{i,n}} \sqrt{\frac{L_{i,n}}{\kappa B T_i}} e^{-j \frac{2\pi}{\lambda} d_{i,n}}$$

$$g^{(tx)}(u, v) = g_E(u, v) \sum_{m=1}^{N_H} \sum_{q=1}^{N_V} e^{jk_0(m d_H u + q d_V v)}$$

$$L_i = L_{sha,i} + L_{atm,i} + L_{sci,i} + L_{CL,i}$$





# System model

- The signal received by the  $k_{th}$  user can be expressed as follows:

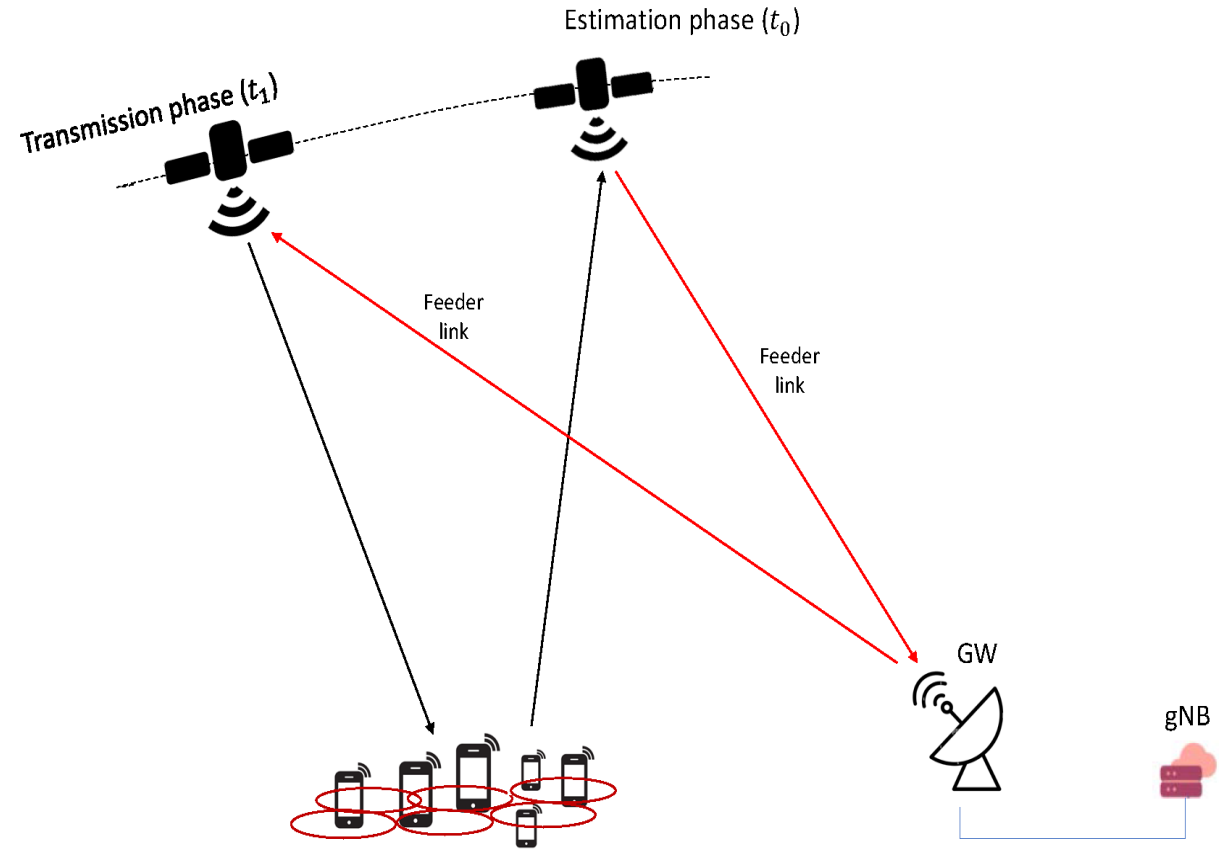
$$y_k = \underbrace{\mathbf{h}_k \mathbf{W}_{:,k} s_k}_{\text{intended}} + \underbrace{\sum_{i=1, i \neq k}^{K_{sch}} \mathbf{h}_k \mathbf{W}_{:,i} s_i}_{\text{interfering}} + z_k$$

$$\mathbf{y} = \mathbf{H}_{t_1} \mathbf{W}_{t_0} \mathbf{s} + \mathbf{z}$$

$\mathbf{H}_{t_1}$  → Scheduled Channel matrix  
 $K_{sch} \times N$

$\mathbf{W}_{t_0}$  → Beamforming Matrix  
 $N \times K_{sch}$

$\mathbf{s} = [s_1, \dots, s_{K_{sch}}]^T$





## CSI based Algorithms

- ZF

$$\mathbf{W}_{ZF} = (\mathbf{H}^H \mathbf{H})^\dagger \mathbf{H}^H$$

- MMSE (RZF)

$$\mathbf{W}_{MMSE} = \arg \min_{\mathbf{W}} E ||\mathbf{H}\mathbf{W}\mathbf{s} + \mathbf{z} - \mathbf{s}||^2$$

$$\mathbf{W}_{MMSE} = \mathbf{H}(\mathbf{H}\mathbf{H}^H + \text{diag}(\boldsymbol{\alpha})\mathbf{I}_{K_{sch}})^{-1}$$

## User's location algorithm

- MB

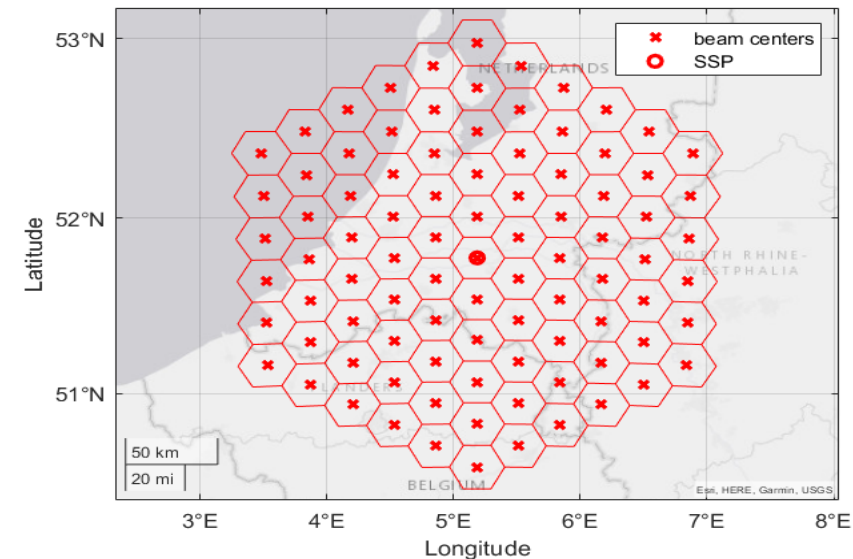
$$\mathbf{B} = [\mathbf{b}_1, \dots, \mathbf{b}_q, \dots, \mathbf{b}_S]$$

$$\mathbf{W}_{MB} = [\mathbf{W}_{:,1}, \dots, \mathbf{W}_{:,q}, \dots, \mathbf{W}_{:,S}]$$

where

$$\mathbf{W}_{:,k} = \mathbf{B}_{:,j}$$

$$j = \arg \min_{i=1, \dots, N} ||\mathbf{C}_i - \mathbf{P}_k||^2$$





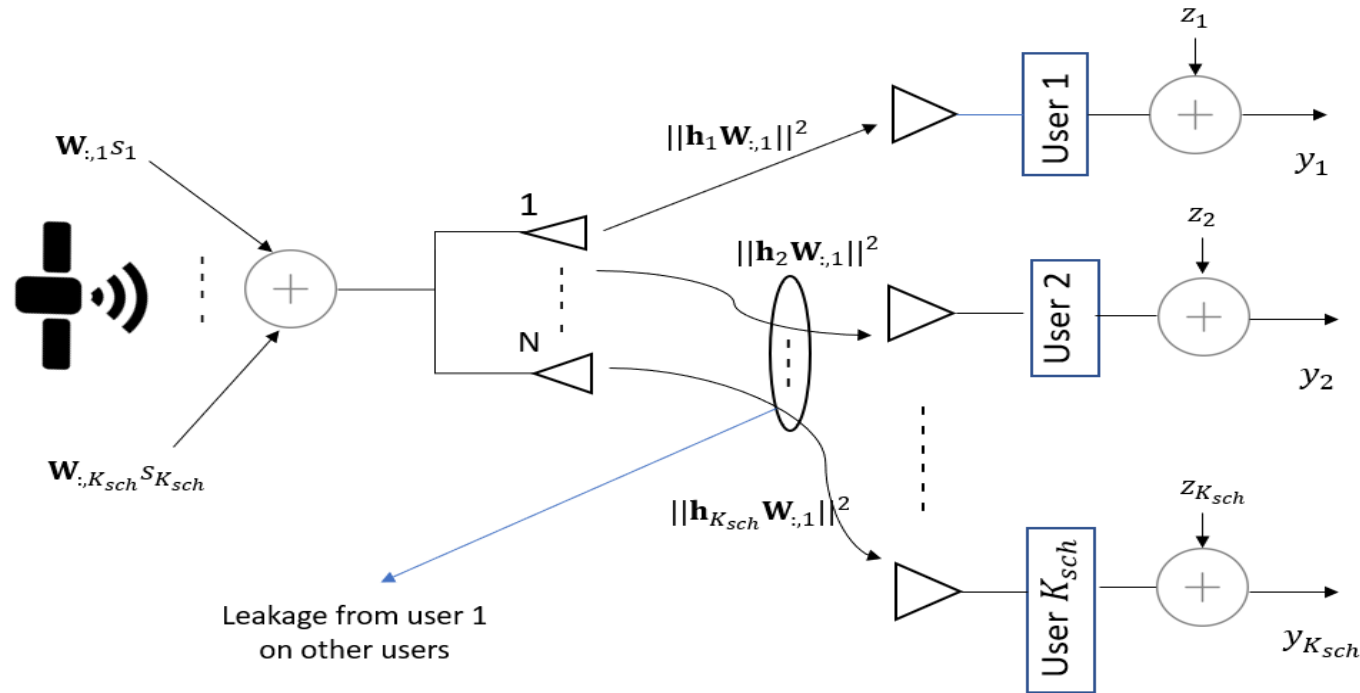
# The Proposed SLNR-based Beamforming

The main motivation is to overcome

- The problem of maximizing SINR for all users
- No closed form solution of the optimization problem (the beamformers are jointly optimized)

$$\text{SLNR}_k = \frac{\|\mathbf{h}_k \mathbf{W}_{:,k}\|^2}{1 + \sum_{i=1, i \neq k}^{K_{sch}} \|\mathbf{h}_i \mathbf{W}_{:,k}\|^2}$$

$$\text{SINR}_k = \frac{\|\mathbf{h}_k \mathbf{W}_{:,k}\|^2}{1 + \sum_{i=1, i \neq k}^{K_{sch}} \|\mathbf{h}_i \mathbf{W}_{:,i}\|^2}$$





# The Proposed SLNR-Based Beamforming

$$\text{SLNR}_k = \frac{||\mathbf{h}_k \mathbf{W}_{:,k}||^2}{1 + \sum_{i=1, i \neq k}^{K_{sch}} ||\mathbf{h}_i \mathbf{W}_{:,k}||^2}$$

$$\text{SLNR}_k = \frac{||\mathbf{h}_k \mathbf{W}_{:,k}||^2}{1 + ||\mathbf{Z}_k \mathbf{W}_{:,k}||^2} \quad \text{where} \quad \mathbf{Z}_k = [\mathbf{h}_1 | \cdots | \mathbf{h}_{k-1} | \mathbf{h}_{k+1} | \cdots | \mathbf{h}_{K_{sch}}]$$

- The beamforming matrix targeted for the user k that maximizes its SLNR is given by:

$$\hat{\mathbf{W}}_{:,k} = \arg \max_{\mathbf{W}} \text{SLNR}_k = \arg \max_{\mathbf{W}} \frac{||\mathbf{h}_k \mathbf{W}_{:,k}||^2}{1 + ||\mathbf{Z}_k \mathbf{W}_{:,k}||^2}$$

- The optimal beamformer is linked to closed-form solution of the generalized eigenvalue problem

$$\hat{\mathbf{W}}_{:,k} \propto \text{max.eigenvector}((1 + \mathbf{Z}_k^H \mathbf{Z}_k)^{-1} \mathbf{h}_k^H \mathbf{h}_k) \longrightarrow \text{SLNR} = \lambda_{max}$$





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# Performance Evaluation Through Numerical Results and Simulation



- A comparative analysis are shown using the following parameters as system KPIs:

✓ Signal to Noise and Interference Ratio (SINR)

$$SINR_k = \frac{SNR_k}{1 + INR_k}$$

✓ Spectral Efficiency (Rate)

$$\eta_k = \log_2(1 + SINR_k)$$

**Power normalization:** power that can be emitted by both the satellite and per antenna

**SPC Normlization**

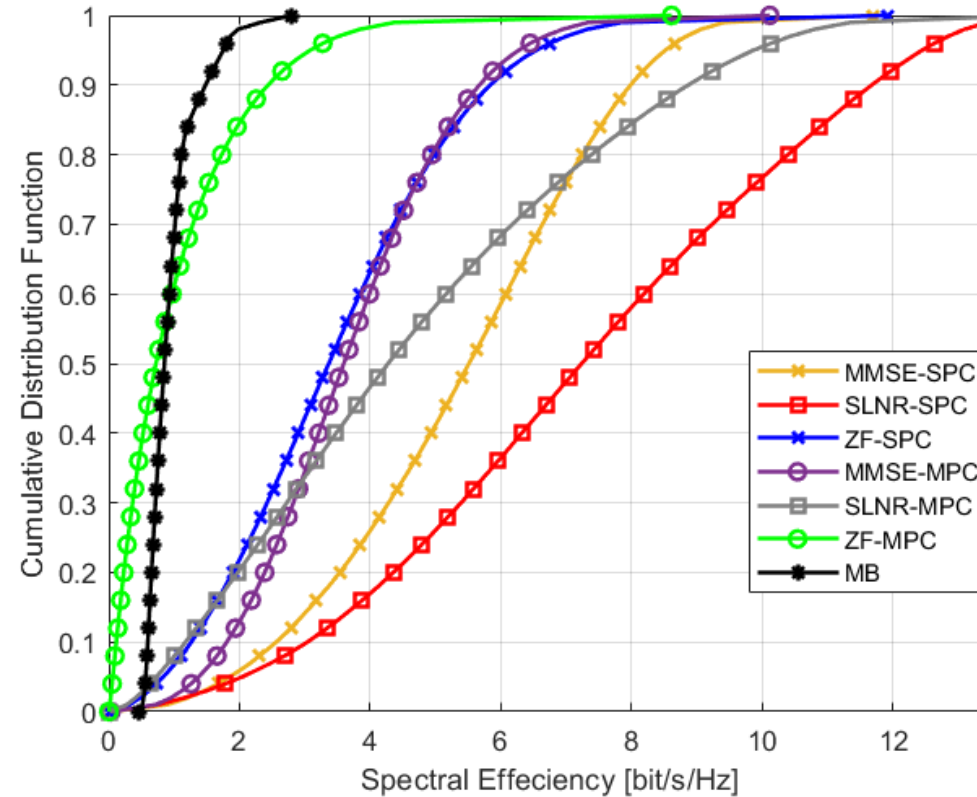
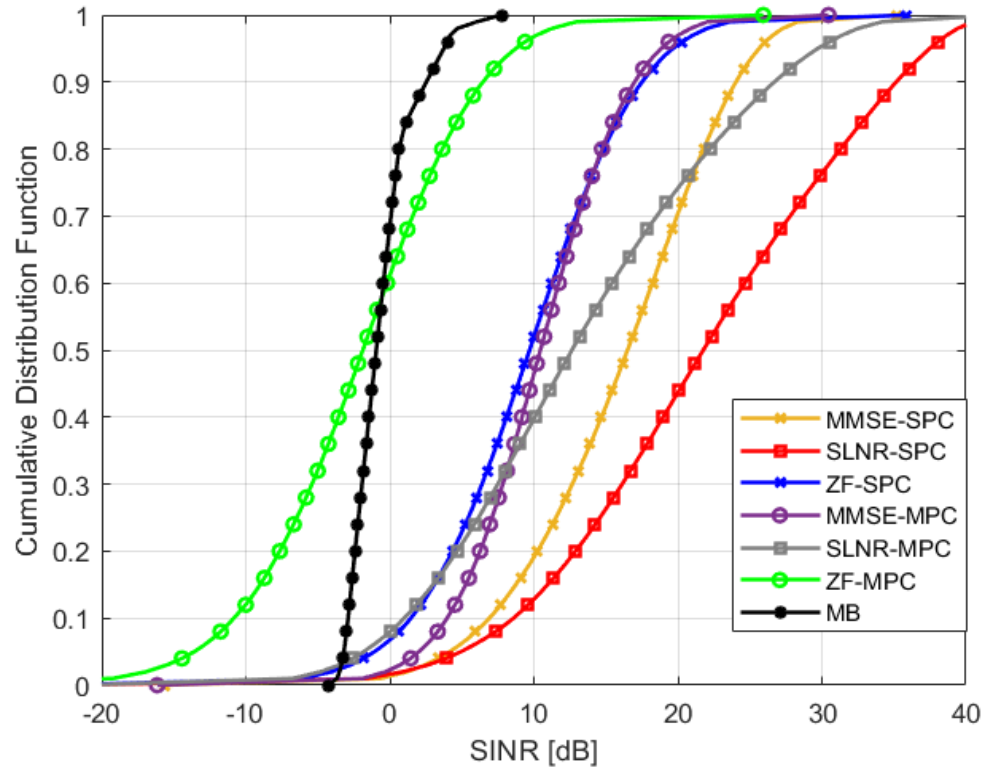
- upper bound is imposed on the total on-board power
- Orthogonality is preserved

**MPC Normalizaation**

- The power per antenna is upper bounded
- Not the entire available on-board power is exploited

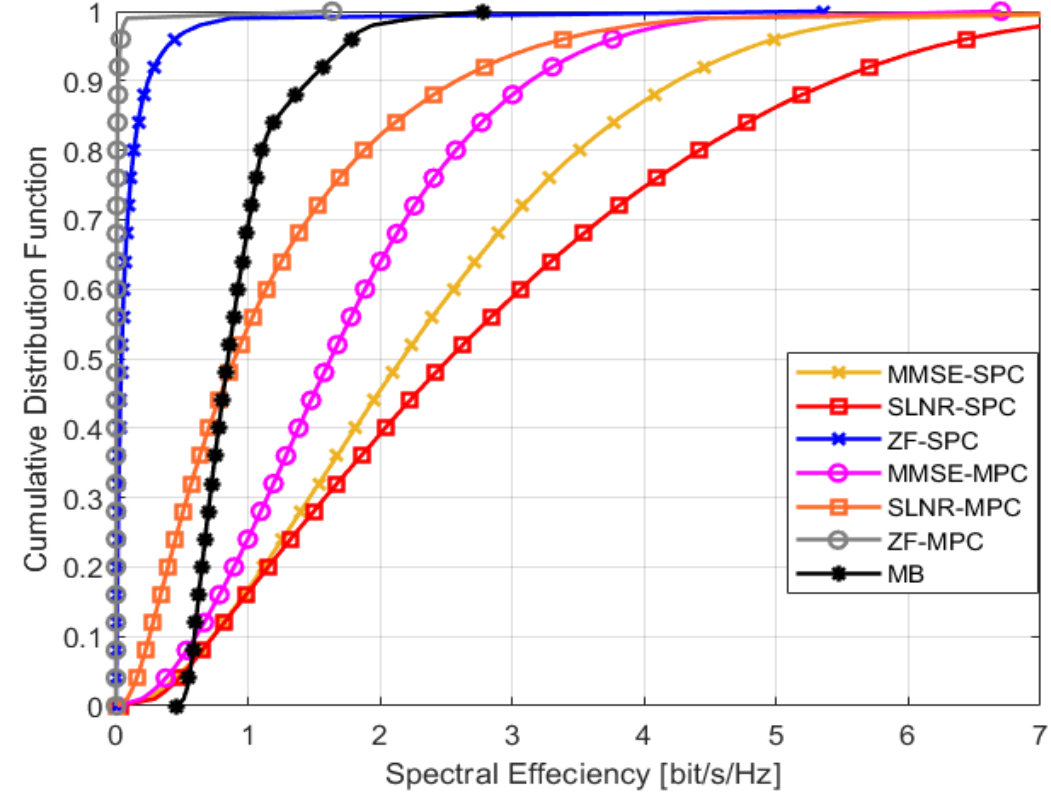
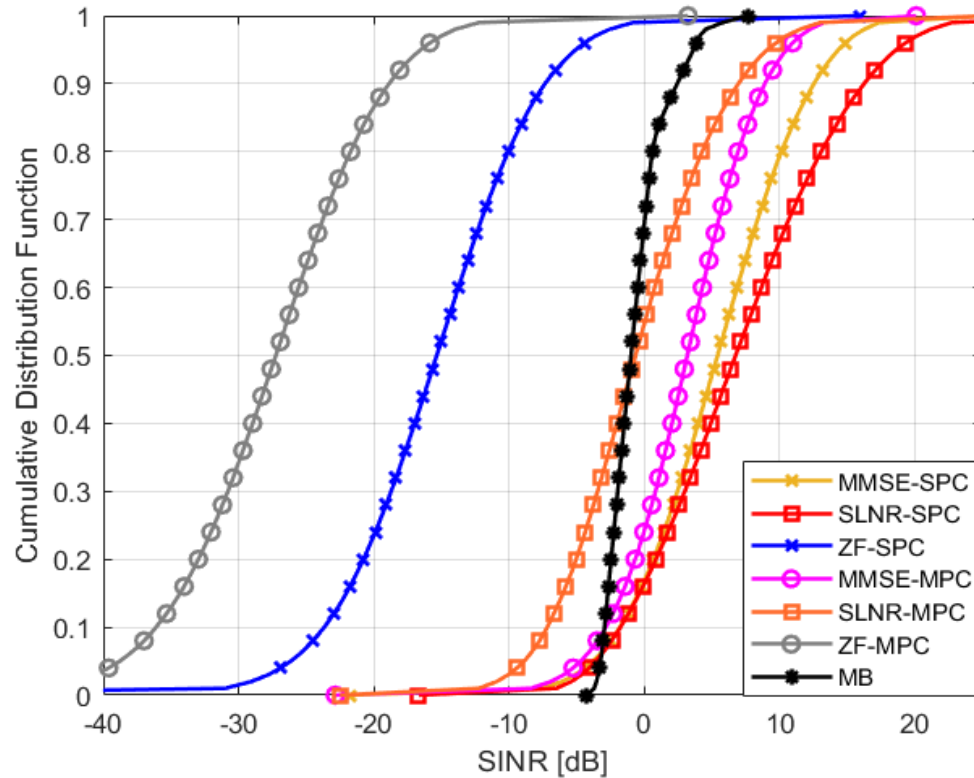
Parameter	Range
Carrier frequency	2GHz
System Band	S band (30 MHz)
Beamforming space	Feed
Receiver type	VSAT
Receiver scenario	Fixed
Propagation scenario	LOS, NLOS
System scenario	Urban
Number of tiers	5
Number of beams	91
Num. of scheduled users	91
Number of transmitters	1024
User density	0.5 users/ $Km^2$





- The proposed SLNR beamforming provides better performance than MMSE, followed by ZF and MB
- In terms of normalization, SPC shows a good results for all beamforming schemes





- The proposed SLNR beamforming provides better performance than MMSE, followed by MB and ZF (is the worst)
- In terms of normalization, SPC shows a better results for all beamforming schemes, followed by MPC and PAC.



# The Proposed SLNR-based Beamforming

## SLNR based beamforming

- considering noise power in implementing beamforming vectors 😊
- Is a regularized channel inversion scheme, with regularization factors customized to each user based on their operating SNR 😊

## ZF beamforming

- not considering noise power in implementing beamforming vectors

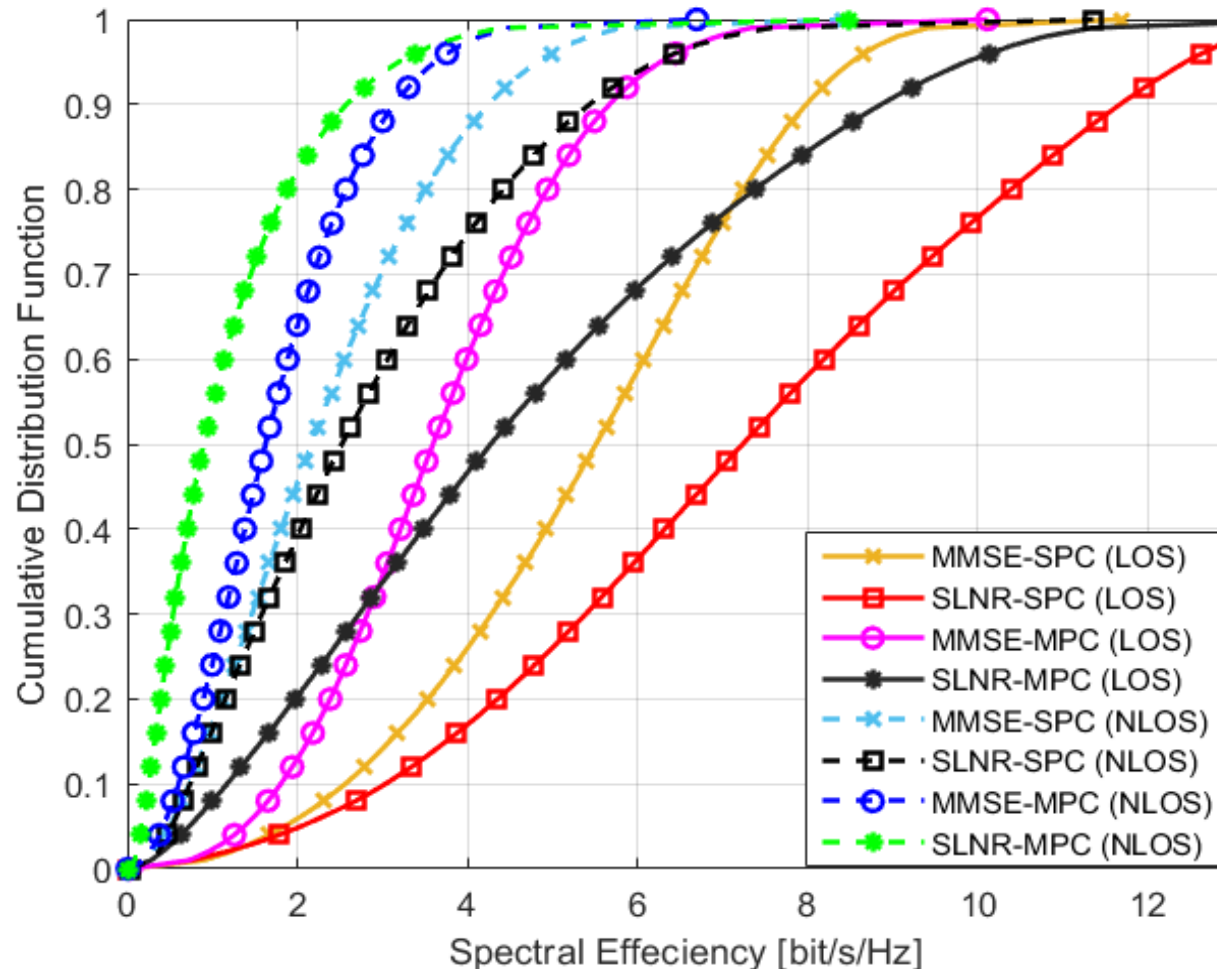
➡ Noise enhancement 😞

## MMSE beamforming

- the same regularization for all users (factor equal to the inverse of average SNR) 😞



# Comparison **LOS** and **NLOS** scenario



Degradation in the performance when moving from LOS to NLOS scenario

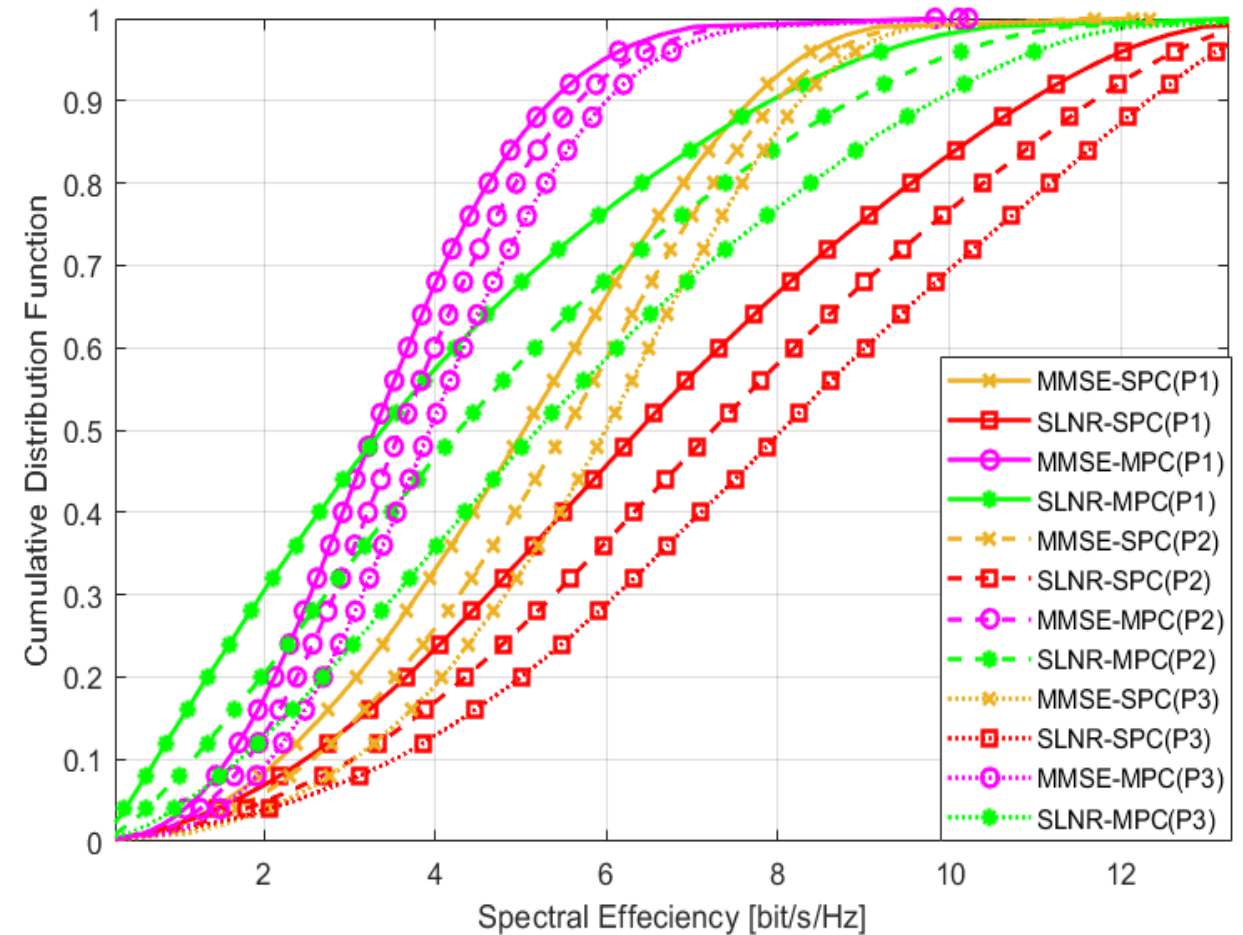
- In the order of 4-5 bit/s/Hz for SLNR-based beamforming
- In the order of 3-4 bit/s/Hz for MMSE-SPC and 1-2 bit/s/Hz for MMSE-MPC.



# Performance assessment at different transmitted power densities $P_t = \{1, 4, 7\}$ dBW/MHz, LOS scenario

By doubling the transmitted power :

- for SLNR scheme, gain in the order of 0.85-0.95 bit/sec/Hz
- for MMSE in order 0.4-0.5 bit/sec/Hz
- such results give additional advantage of the proposed scheme.





- Proposing a beamforming algorithm aimed at maximizing the figure of merit (SLNR)
- SLNR-based scheme eliminates the joint coupling between the beamforming vectors into multiple separate optimization problems of the targeting users
- System level assessment and comparison with benchmark solutions
  - CSI-based
  - Location-based
- The numerical results provided a significant better performance of SLNR-based beamforming than the optimal MMSE followed by MB and ZF beamforming in terms of spectral efficiency and SINR
- The power normalization SPC introduced the best performance for all beamforming algorithms followed by MPC
- Degradation in the performance when moving from LOS to NLOS propagation scenario
- The increased transmitted power density introduced slight improvement for SLNR and MMSE beamforming
- **Future Works**: considering multiple satellites in a mega-constellation scenario ➡ global coverage





**H2020 DYNASAT:** (Dynamic spectrum sharing and bandwidth-efficient techniques for high-throughput MIMO Satellite systems)

- Research, develop, and demonstrate techniques for **bandwidth efficient transmission** and **efficient spectrum usage** for a **high throughput 5G/6G Satellite** access network infrastructure, based on advanced NGSO-mega-constellation



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**Thank you for your attention**

**Rabih Dakkak**

Department of Electrical, Electronic and Information  
Engineering «Guglielmo Marconi»

mrabih.dakkak2@unibo.it

[www.unibo.it](http://www.unibo.it)